

## College Algebra Exam Formulas Sheet

Some equation forms of a line:

$$y = mx + b$$

$$y - y_1 = m(x - x_1)$$

$$Ax + By = C$$

Some equation forms of a circle:

$$(x - h)^2 + (y - k)^2 = r^2$$

$$x^2 + y^2 + ax + by + c = 0$$

Given a line passing through points  $(x_1, y_1)$  and  $(x_2, y_2)$ , the slope  $m$  of the line is  $m = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1}$  as long as  $x_2 \neq x_1$

The average rate of change of a function from  $a$  to  $b$  is  $\frac{f(b) - f(a)}{b - a}$

Some equation forms of a parabola:

$$y = f(x) = a(x - h)^2 + k$$

$$y = ax^2 + bx + c, \text{ with vertex } \left(-\frac{b}{2a}, c - \frac{b^2}{4a}\right)$$

The Law of Exponents:

Given  $a > 0$  with  $a \neq 1$ : If  $a^u = a^v$ , then  $u = v$ .

### SUMMARY Properties of Logarithms

In the list that follows,  $a, b, M, N$ , and  $r$  are real numbers. Also,  $a > 0, a \neq 1, b > 0, b \neq 1, M > 0$ , and  $N > 0$ .

#### Definition

$$y = \log_a x \text{ means } x = a^y$$

#### Properties of logarithms

$$\log_a 1 = 0; \quad \log_a a = 1$$

$$\log_a M^r = r \log_a M$$

$$a^{\log_a M} = M; \quad \log_a a^r = r$$

$$a^x = e^{x \ln a}$$

$$\log_a(MN) = \log_a M + \log_a N$$

$$\text{If } M = N, \text{ then } \log_a M = \log_a N.$$

$$\log_a\left(\frac{M}{N}\right) = \log_a M - \log_a N$$

$$\text{If } \log_a M = \log_a N, \text{ then } M = N.$$

#### Change-of-Base Formula

$$\log_a M = \frac{\log_b M}{\log_b a}$$

The compound interest formula states that  $F = P \left(1 + \frac{r}{n}\right)^{nt}$

The continuously compounded interest formula states that  $F = Pe^{rt}$

The exponential law states that an amount  $A$  varies with time  $t$  according to the function  $A(t) = A_0 e^{kt}$   
As long as the start time is 0, the value of  $k$  can be determined using the adder  $a$  and either the multiplier  $m$  or the divider  $d$ :

$$\boxed{k = \frac{\ln m}{a}} \quad \text{or} \quad \boxed{k = \frac{\ln(1/d)}{a}}$$